

OF TECHNOLOGY

Individualised summative assignments [that can be scaled sustainably] FYi Maths workshop — 2018

Dr. Ant Edwards

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28 June, 2018

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How do we decide how to assess understanding in first year mathematics?

Quality of assessment

Authenticity of assessment









A form of assessment in which students are asked to perform real-world tasks that demonstrate meaningful application of essential knowledge and skills (Mueller, 2005, p. 1).







Performance assessments call upon the examinee to demonstrate specific skills and competencies, that is, to apply the skills and knowledge they have mastered (Stiggins, 1987, p. 34).













The distance between the actual developmental level as determined by independent problem solving and the level of potential development as determined through problem-solving under adult guidance, or in collaboration with more capable peers (Vygotsky, 1978, p. 86).





Quality of assessment

Identity verification























Quality of assessment

- Authenticity of assessment
- Academic challenge
- Identity verification
- Replicability
- Scalability
- Sustainability





Time & Resourcing

- student time
- marking staff time
- teaching staff time
- support staff time
- convening staff time





The problem:



How do we decide how to assess understanding in first year mathematics?

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These are related to scaleability and sustainability.

Features of an automated solution

We want to maximise quality while keeping within time and resourcing constraints

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SW

Can technology help?





Can technology help?



Potentially.



Can technology help?

Potentially, depends on context.





Can technology help?





Potentially, depends on context.

Today I am talking about assessments that are:

Medium-stakes (10-20%)

Can technology help?





Potentially, depends on context.

- Medium-stakes (10-20%)
- ► First-year, mid semester

Can technology help?





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- "authentic"

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Potentially, depends on context.

- Medium-stakes (10-20%)
- ► First-year, mid semester
- "authentic"
- Each student has a slightly different problem to solve

Can technology help?





Potentially, depends on context.

- Medium-stakes (10-20%)
- ► First-year, mid semester
- "authentic"
- Each student has a slightly different problem to solve
- Multiple-approaches possible



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Example 1

Example 1: MTH10008 Aviation Mathamtics

Background

Unit for two groups of students

- BSc. Aviation (piloting)
- BSc. Aviation Management

"Piecemeal" areas of study: vectors, complex numbers, calculus, finance, descriptive statistics, probability.

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Discounted cash flow analysis — TI84 required

15. [06 marks] A company plans to invest \$1,000,000 in a new plant. Their accountant makes the following net cash flow projections on the investment. The final cash flow in year 4 includes a residual value. The cost of capital is 8% over the life of the investment project.

Year	NET CASH FLOWS
0	(\$1,000,000)
1	\$200,000
2	\$250,000
3	\$300,000
4	\$550,000

(a) Calculate the Net Present Value (NPV) and Internal Rate of Return (IRR) of this investment plan. [4 marks]





Consultation with aviation academics and industry



- Consultation with aviation academics and industry
- Identified "real-life" situation



- Consultation with aviation academics and industry
- Identified "real-life" situation



New mining operation

- Different options for routes
- Many different constraints
- Messy, nonlinear brief
- Produce a business case for the airline's shareholders

Bangula, Malawi

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Using Excel to produce variables for n students.

1 Keep the "key" values in one tab


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- @ Use another tab with a single frozen row to randomise by a multiplicative factor of $\pm \frac{\delta}{2}$



- Keep the "key" values in one tab
- 2 Use another tab with a single frozen row to randomise by a multiplicative factor of $\pm \frac{\delta}{2}$
 - =cell*(1+ δ *rand()- $\delta/2$)



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- \bigcirc Fill down from this row n times



- Keep the "key" values in one tab
- 2 Use another tab with a single frozen row to randomise by a multiplicative factor of $\pm \frac{\delta}{2}$
 - =cell*(1+ δ *rand()- δ /2)
- **3** Fill down from this row n times
- 4 Immediately copy and "paste as values" on top of row 2 to (n+1)



- 1 Use another tab to check answers
 - e.g. Extreme cases



- 1 Use another tab to check answers
 - e.g. Extreme cases
- 2 Potentially use this tab also to create dependencies



1 Format as much as possible in Excel first



1 Format as much as possible in Excel first

2 Testing and "post-production" formatting in Word

Format	Excel	Word	
percentage	50%	0.5	
Currency	\$12.50	12.5	
Telephone	039145393	39145393	

https://knowledgecenter.zuora.com/CB_Billing/IA_Invoices/Creating_a_Custom_Invoice_Template/B_

Define_the_Format_for_Date_and_Number_Fields



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Define_the_Format_for_Date_and_Number_Fields

8 Use Word to run mailmerge in Outlook



No issues with scaling in terms of rollout (additional marker in 2018)



2017 79 students

2018 106 students

No issues with scaling in terms of rollout (additional marker in 2018)

Issues

Open-ended nature

- issues with "what to do"
- clarifications after marking
- difficult to mark students who had gone off-piste
- Marking relied still involved manual checking of spreadsheet



No issues with scaling in terms of rollout (additional marker in 2018)

Issues

Open-ended nature

- issues with "what to do"
- clarifications after marking
- difficult to mark students who had gone off-piste
- Marking relied still involved manual checking of spreadsheet

Benefits

- It seemed to work (!)
- No student questioned value of assessment
- Students seeking help were genuinely engaged with the project

Example 2: MTH10010 Essential Mathematics

Background

From c.2005–2015 we taught a "one-stop shop" for entry-level mathematics

- For students without Mathematics Methods entry
- For students taking their last mathematics unit at University ("terminal" students)

This was bad for both groups...

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Example 2: MTH10010 Essential Mathematics

Background

In 2015 we split these into two units.

Essential Mathermatics is the "terminal" unit, written from scratch (by me)

My approach

Example 2



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Example 2

- Mathematics Methods (or equivalent) requirement
- Primarily BSc Science students
- Functions, Statistics, Calculus



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Example 2

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Example 2: MTH10010 Essential Mathematics

Background

Statistics taught in **R** labs.

- Practical focus
- ▶ Using **R** to calculate descriptive stats, correlation, regression
- meaning of terms such as effect size, power in inferential statistics (t-tests only)
- Hybrid individual-group assignment (milestones from week 8 onwards)



Example 2

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Example 2: MTH10010 Essential Mathamtics

Background

Statistics taught in **R** labs.

- Practical focus
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Descriptive statistics in R

The final part of my daily commute is travelling to level 7 of the EN building. Once I go through the main entrance I must then must choose how to reach my office opposite lecture theatre EN715. I can take the lift, which is slow but quite consistent in its journey time. The escalators are faster—especially if I walk up them—but congestion sometimes makes this frustratingly slow.

For your individual project you will be given timing data on these routes. This task involves you preparing some descriptive statistics for me in the form of a written report.

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- Each student received 30 paired data points (15 per route)
- Matlab generated the data for n students
 - Set up array of size $15 \times 2 \times n$
 - One distribution was randomly sampled from known data $N(\bar{x}, s^2)$ (makedist, truncate to eliminate impossible times, then random)
 - Other distribution was randomised from the first, point by point
 - (rand with a similar setup to before)



- **1** Matlab code generated the descriptive statistics and graphs
- **2** Published to a pdf document for the marker

		My approach	Example 2
measure	escalator	lift	
'mean'	[133.8335]	[189.8259]	
'std'	[27.7930]	[40.3288]	
'min'	[101.9139]	[110.0907]	
'01'	[104.4371]	[169.6255]	
'med'	[133.6007]	182.86691	
'03'	[155.0967]	[225.1733]	
'max'	[183.3910]	[246.6303]	

correlation =

0.6349



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Individualised Assessments



Generate csv file from Matlab (using array2table and writetable)
Then, as before



Cohort size [assignments submitted]

2017 59 students



Cohort size [assignments submitted]

2017 59 students

Issues

- Lots of clicking to set up mail-merge
- Wrong answers:

there are different ways of calculating percentiles

 Limited value for repeating students



2017 59 students

Issues

- Lots of clicking to set up mail-merge
- Wrong answers:

there are different ways of calculating percentiles

 Limited value for repeating students

Benefits

- Quick to mark
- Good feedback from the marker
- Worked well throughout
- Very scalable
- Can easily be expanded to auto mark numerical answers











Mail-merge based approach reflections

Two strategies for individualised assessments have been presented:



Mail-merge based approach reflections

Two strategies for individualised assessments have been presented:

- Mail-merge using Excel, Word and Outlook
- Mail-merge using Matlab, Excel, Word and Outlook

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Summary

Mail-merge based approach reflections

Two strategies for individualised assessments have been presented:

- Mail-merge using Excel, Word and Outlook
- ► Mail-merge using Matlab, Excel, Word and Outlook
- Mail-merge using <package> and <productivity suite>

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Mail-merge based approach reflections

Two strategies for individualised assessments have been presented:

- Mail-merge using Excel, Word and Outlook
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Quality of assessment

- Authenticity of assessment
- Academic challenge
- Identity verification
- Replicability
- Scalability
- Sustainability

Time & Resourcing

- student time
- marking staff time
- teaching staff time
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- convening staff time

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Summary

Mail-merge based approach reflections

Two strategies for individualised assessments have been presented:

- Mail-merge using Excel, Word and Outlook
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Other approaches





Other approaches

Numbas

Other approaches



One package to do all of them, via the VLE?

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NUMBAS

Other approaches

Numbas



Numbas

Numbas

NUMBAS

https://www.numbas.org.uk

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Numbas



Numbas

 Free, open-source, online question engine

NUMBAS



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- Emphasis on easy creation of questions

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- Can be run in VLEs via standalone SCORM package

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NUMBAS

- not designed for summative assessment
- issues with student tracking and answer tracking in SCORM (in particular, Blackboard)
- "creative, problem-solving tasks are much harder to automate and repeat" (Perfect, 2015)

Personalised dataset & auto-marked questions requiring use of ${\bf R}$

```
University of Newcastle, Dr Lee Fawcett
https:
//numbas-editor.mas.ncl.ac.uk/numbas-previews/
exam-1879-mas1802-practical-1/index.html
```

Randomised Discount Cash Flow question

Cork Institute of Technology, Dr Julie Crowley https://numbas.mathcentre.ac.uk/question/13303/ net-present-value-2/

Searching the Numbas public database

https://numbas.mathcentre.ac.uk/search/

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Individualised Assessments











All-in-one system such as Pearson MyMathLab, Numbas

Quality of assessment

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- 🗸 Scalability
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Time & Resourcing

- ? student time
- ✓ marking staff time
- ✓ teaching staff time
 - ? support staff time
- × convening staff time

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Other approaches





Auto Multiple Choice (LATEX)





Auto Multiple Choice (LATEX)

Free, open-source Latex package





Auto Multiple Choice (LATEX)

- Free, open-source Latex package
- Can generate individualised tests and answers





Auto Multiple Choice (LATEX)

- Free, open-source Latex package
- Can generate individualised tests and answers
- Paper-based





Auto Multiple Choice (LATEX)

- Free, open-source Latex package
- Can generate individualised tests and answers
- Paper-based
- Built-in auto-marking





Auto Multiple Choice (LATEX)

- Free, open-source Latex package
- Can generate individualised tests and answers
- Paper-based
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```
https://www.
auto-multiple-choice.net
```





Auto Multiple Choice (LATEX)

- Free, open-source Latex package
- Can generate individualised tests and answers
- Paper-based
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Multiple Choice sheets automated marking

 requires knowledge of Latex (variables are handled by pgfmathparse).



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- Can generate individualised tests and answers
- Paper-based
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Multiple Choice sheets automated marking

- requires knowledge of Latex (variables are handled by pgfmathparse).
- requires basic knowledge of python



Auto Multiple Choice (LATEX)

- Free, open-source Latex package
- Can generate individualised tests and answers
- Paper-based
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https://www. auto-multiple-choice.net



Multiple Choice sheets automated marking

- requires knowledge of Latex (variables are handled by pgfmathparse).
- requires basic knowledge of python
- main purpose is auto-reading of scanned multiple choice answers



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Classe d'application d'AMC

Examen du 01/01/2010

Cet examen a pour but d'illustrer l'utilisation d'Auto Multiple Choice. Vous pourrez trouver sur le site d'AMC les copies de Jojb Boulix et André Roullet afin de tester la saisie automatique, ainsi que le fichier listaut ke étudiants de la dasse d'application d'AMC (dout fort partie Jojo et André) afin de tester l'association automatique à partir des numéros d'étudiants.

Si vous choisissez une note maximale de 10 et l'arrondi normal pour cet examen, Jojo obtiendra la note 5/10 et André la note 6/10.

-
r
ī

← codez votre numéro d'étudiant ci-contre, et écrivez votre nom et prénom ci-dessous.

Nor	n (t	pre	'n	a	n	:										

Les questions faisant apparaître le symbole 🌲 peuvent présenter zéro, une ou plusieurs bonnes réponses. Les autres ont une unique bonne réponse.

Question 1	Un paquet logiciel est fourni sur le site d'AMC. Quel en est le format ?								
	🗌 deb	\Box slp	🗌 rpm	🗆 exe					
Question 2 🌲	Sur quels logicie	ls repose Pimp	démentation d'	AMC version 0.199 ?					
🗌 Gimp			🗌 ImageN	lagick ou GraphicsMagick					
Apache Perl			Firefox						
□ ⊮ī _E x			🗌 Aucune	de ces réponses n'est correcte.					
Question 3	Sous quelle licena	e AMC est-il d	listribué?						
🗌 Licence A	pache		🗌 Licence	commerciale AMC					
🗌 GNU Ger	eral Public License	e V2	🗆 GNU G	eneral Public License V3					

Individualised Assessments

Auto Multiple Choice Summary



Paper-based multiple-choice such as Auto Multiple Choice

Quality of assessment

- ? Authenticity of assessment
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- × Identity verification
- ? Replicability
- ? Scalability
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Time & Resourcing

- ✓ student time
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- ✓ convening staff time

Summary and recommendations



	Mail-merge	Numbas	AMC
Authenticity of assessment	\checkmark	×	?
Academic challenge	\checkmark	\checkmark	?
Identity verification	×	×	×
Replicability	?	?	?
Scalability	\checkmark	\checkmark	?
Sustainability	\checkmark	\checkmark	\checkmark
Student time	\checkmark	?	\checkmark
Marking staff time	?	\checkmark	\checkmark
Teaching staff time	\checkmark	\checkmark	\checkmark
Support staff time	?	?	?
Convening staff time	×	×	\checkmark

Any questions?

My question for you:

What are your experiences with individualised assessments?

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Individualised Assessments

References



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